

Adopt a Polyhedral Compiler!

IMPACT 2013 Workshop

Albert Cohen

INRIA and École Normale Supérieure, Paris
<http://www.di.ens.fr/ParkasTeam.html>

People Have Great Expectations

- Accelerating legacy code for ever
- Simplifying compiler construction and library generation
- Peak performance at the touch of a button
- Proving program transformations
- Code generation for heterogeneous architectures
- High-level circuit synthesis
- Publishing great papers
- [Name your own dream project here]

FREE
LUNCH
ANY ONE?

There Were, and Will Be Times in the Wilderness...



But the World Will Eventually Turn Polyhedral!



Courtesy www.progonos.com/furuti

Lost Memories in the Not-Yet-Polyhedral World

DDR3-2133 SDRAM

Latency: **10.3 ns**

Memory bandwidth: **17.6 GB/s**

4-core 2GHz ARM Cortex A15

Compute bandwidth: $2 \times 4 \text{ threads} \times 1 \text{ NEON unit} \times 16 \text{ bytes} \times 2 \text{ GHz} = \mathbf{1024 \text{ GB/s}}$

8-core 3GHz AMD Opteron

Compute bandwidth: $2 \times 8 \text{ threads} \times 2 \text{ SSE units} \times 16 \text{ bytes} \times 3 \text{ GHz} = \mathbf{1536 \text{ GB/s}}$

Memory bandwidth: **17.6 GB/s**

256-core 400MHz Kalray MPPA

Compute bandwidth: $2 \times 256 \text{ threads} \times 2 \text{ words} \times 4 \text{ bytes} \times 400 \text{ MHz} = \mathbf{1638.4 \text{ GB/s}}$

1536-core 1.006GHz NVIDIA Kepler

Compute bandwidth: $2 \times 1536 \text{ threads} \times 1 \text{ float} \times 4 \text{ bytes} \times 1.006 \text{ GHz} = \mathbf{12361.6 \text{ GB/s}}$

Memory bandwidth: **190 GB/s**

Many Candidates for Adoption

- ▷ **What are the essential semantic requirements for source programs?**
- ▷ **Should programmers care**
 - About parallelism?
 - About the memory and power walls?**Which programmers?**
- ▷ **What role for the software stack?**
 - Compilers
 - Runtime systems
 - Libraries, library generators
 - Auto-tuning, dynamic optimization
 - Operating system, virtual machine monitor
- ▷ **What role for the polyhedral tools?**

**Challenges for a
polyhedral world**

Data-
dependent
control flow,
dynamic
analysis

Scalability,
just-in-time
compilation

Modularity,
genericity,
functional
abstraction

Task-level
optimiza-
tions,
stream-
computing

Domain-
specific
languages

Accelerators,
vectorization,
distributed
memory

State-of-the-Art Tool: PPCG – Polyhedral Parallel Code Generator

PPCG (<http://freecode.com/projects/ppcg>)

- Input: C
- Output:
 - ▶ OpenMP
 - ▶ CUDA
 - ▶ OpenCL (soon)

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- Input: C
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Steps:

- Extract polyhedral model from source code (pet,isl)
- Dependence analysis (isl)
- Scheduling (isl)
 - ▶ Expose parallelism and tiling opportunities
 - ▶ Separate schedule into parts mapped on host and GPU
 - ▶ perform tiling, mapping outer parallel dimensions to blocks and inner parallel dimensions to threads
- Memory management (isl)
 - ▶ Add transfers of data to/from GPU (isl)
 - ▶ Detect array reference groups
 - ▶ Allocate groups to registers and shared memory
- Generate AST (isl)

PPCG Example – Input

Source code:

```
void matmul(int M, int N, int K,
            float A[static const restrict M][K],
            float B[static const restrict K][N],
            float C[static const restrict M][N])
{
    for (int i = 0; i < M; i++)
        for (int j = 0; j < N; j++) {
S1:    C[i][j] = 0;
            for (int k = 0; k < K; k++)
S2:    C[i][j] = C[i][j] + A[i][k] * B[k][j];
        }
}
```

Options:

```
--ctx="[M,N,K] -> { : M = N = K = 256 }"
--sizes="{ kernel[i] -> tile[16,16,16];
           kernel[i] -> block[8,16] }"
```

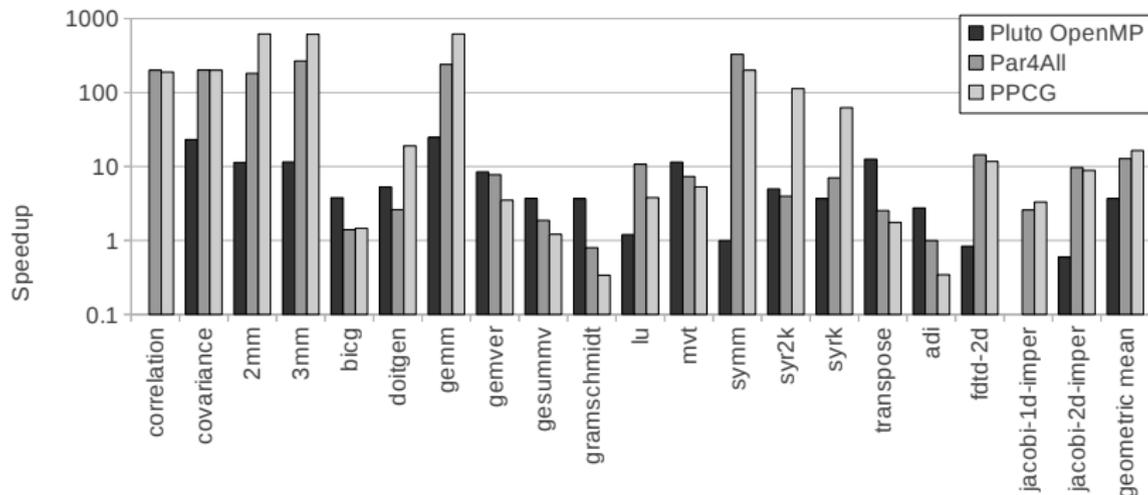
PPCG Example – Output

Kernel code: (host code not shown)

```
int b0 = blockIdx.y, b1 = blockIdx.x;
int t0 = threadIdx.y, t1 = threadIdx.x;
__shared__ float s_A[16][16];
__shared__ float s_B[16][16];
float p_C[2][1];

p_C[0][0] = C[(16 * b0 + t0) * (256) + 16 * b1 + t1];
p_C[1][0] = C[(16 * b0 + t0 + 8) * (256) + 16 * b1 + t1];
for (int g9 = 0; g9 <= 240; g9 += 16) {
    for (int c0 = t0; c0 <= 15; c0 += 8)
        s_B[c0][t1] = B[(g9 + c0) * (256) + 16 * b1 + t1];
    for (int c0 = t0; c0 <= 15; c0 += 8)
        s_A[c0][t1] = A[(16 * b0 + c0) * (256) + t1 + g9];
    __syncthreads();
    if (g9 == 0) {
        p_C[0][0] = (0);
        p_C[1][0] = (0);
    }
    for (int c2 = 0; c2 <= 15; c2 += 1) {
        p_C[0][0] = (p_C[0][0] + (s_A[t0][c2] * s_B[c2][t1]));
        p_C[1][0] = (p_C[1][0] + (s_A[t0 + 8][c2] * s_B[c2][t1]));
    }
    __syncthreads();
}
C[(16 * b0 + t0) * (256) + 16 * b1 + t1] = p_C[0][0];
C[(16 * b0 + t0 + 8) * (256) + 16 * b1 + t1] = p_C[1][0];
```

PPCG Results



- Benchmarks: PolyBench 3.1
- Platform: Tesla M2070
- Baseline: sequential CPU execution `gcc -Ofast`

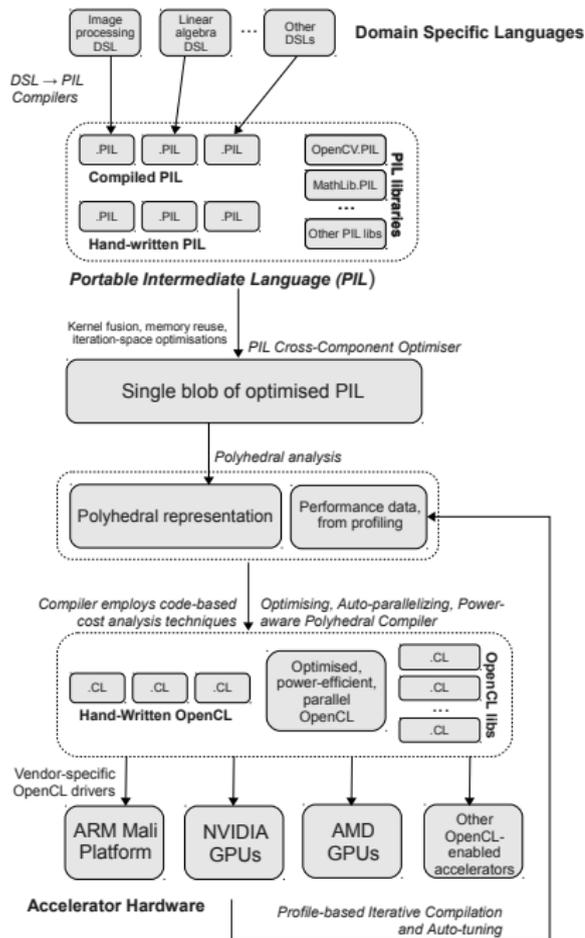
Attend Carlos Juega's talk on Wednesday morning!

CARP EU Project



w/ ARM, RealEyes, Rightware, Monoidics,
Imperial College, RWTH Aachen, U. Twente

- Compiler construction for DSLs:
support for parallelization,
vectorization, loop transformation...
- Reconcile advanced loop nest
optimizations and software
engineering practices

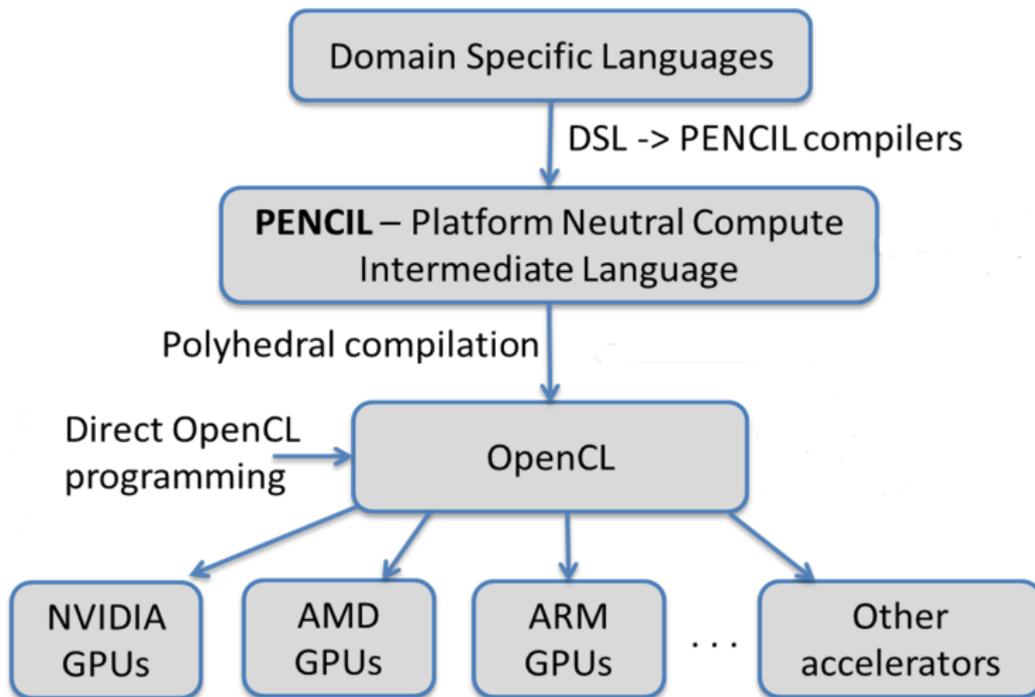


DSLs to the Rescue

- **Problem:** general purpose languages are not optimization-friendly
 - ▶ much static semantics is lost
 - ▶ much domain information is lost
 - ▶ high expressiveness → ambiguitis disable optimizations (e.g., pointer aliasing)
- Some DSLs are designed primarily for abstraction and productivity
→ we are interested in the performance-focused DSLs

- **But** compiling DSLs directly into OpenCL or CUDA is not advisable
- **Approach:** target an appropriate intermediate language (IL) and leverage a generic optimization framework

Zooming in on Pencil



Pencil: a Platform-Neutral Compute Intermediate Language

An intermediate language for DSL compilers

- C-based intermediate language
- Code regions specifically marked as PENCIL-compliant
- Sequential, platform neutral
- A set of coding rules, language extensions and directives
- Planning for an LLVM IR version of PENCIL
- Complementary objectives to DSL intermediate languages such as Delite IR

Design goals

- **Unlock** the power of optimization frameworks by
 - ▶ keeping a maximum of information expressed by the DSL
 - ▶ eliminating ambiguity for optimizers
- **Users:** Code generators + expert developers

Platform-Neutral Compute Intermediate Languages

- Coding rules for PENCIL functions
- Language extensions (C11-compatible)
- Directives

Platform-Neutral Compute Intermediate Languages

- Coding rules for PENCIL functions
 - ▶ cannot be recursive
 - ▶ no `gotos`
 - ▶ no pointers
 - ▶ array arguments should be declared with `static const restrict` inferred through automatic versioning
 - ▶ dedicated types and builtins for dynamic analysis (work in progress)
- Language extensions (C11-compatible)

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- Language extensions (C11-compatible)
 - ▶ access summary functions
 - ▶ describe access pattern of a function if static analysis cannot be performed (no source or not PENCIL compliant) or if the results are too inaccurate
 - ▶ modular interprocedural information used in the caller through “polyhedral inlining”
- Directives

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 - ▶ modular interprocedural information used in the caller through “polyhedral inlining”

- Directives

- ▶ `#pragma pencil independent [(l1, ..., ln)]`

listed statements (all if unspecified) do not carry any dependences across the loop following the directive

Example of Pencil code

```
int function(int A[static const restrict 100][100],
            int C[static const restrict 100][100]) {
    #pragma pencil independent
    for (int k = 0; k < N; k++)
        for (int j = 0; j < N; j++)
            A[k][t[j]] = foo(C);
}
```

Example of Pencil code

```
void foo_summary(int C[static const restrict n][n]) {
    for (int i=0; i<n; i++)
        USE(C[i]); // marks row i of C as being read
}

void foo(int C[const restrict n][n])
    ACCESS(foo_summary(C));

int function(int A[static const restrict 100][100],
             int C[static const restrict 100][100]) {
    #pragma pencil independent
    for (int k = 0; k < N; k++)
        for (int j = 0; j < N; j++)
            A[k][t[j]] = foo(C);
}
```

Modularity, Genericity, Functional Abstraction, and DSLs

- Short-term

- ▶ Functional abstraction → inlining
- ▶ Genericity → specialization, partial evaluation
- ▶ Modularity → staged programs: write program generators
- ▶ ... a roadmap for a DSL compiler builder
cf. NumPy, pythran, C++ template metaprogramming (TaskGraph library, RapidMind/ArBB), Delite (Scala), Halide, OP2, MetaOCaml experiments...

- Long-term

- ▶ Support function-level fusion, vectorization, tiling
cf. Kennedy's Telescoping Languages
- ▶ On-demand function cloning rather than inlining

What Else Do You Want From a Polyhedral Compiler?

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Complex transformations

Scalability

Just-in-time and split compilation

Auto-tuning

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Complex transformations

Scalability

Just-in-time and split compilation

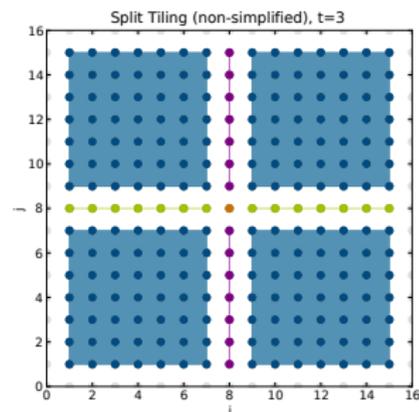
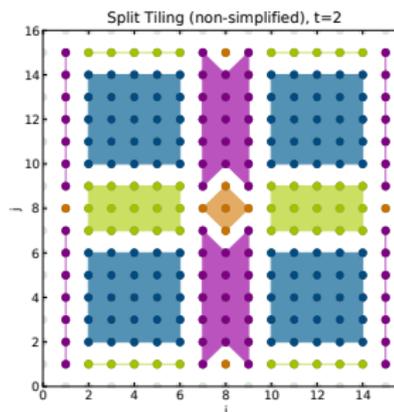
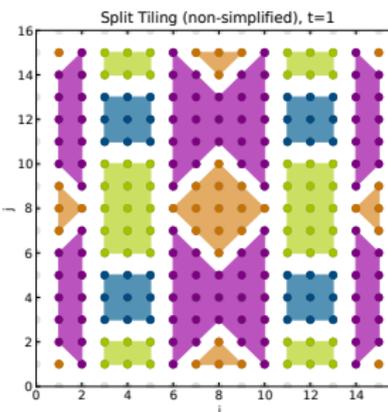
Auto-tuning

Dynamic analysis, optimistic transformations

Adaptation and optimization of parallel code

Complex Transformations

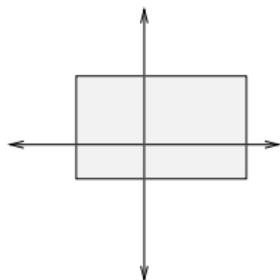
E.g., **split tiling**, diamond tiling, overlapped tiling...



More complex?

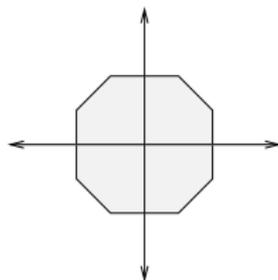
- Instancewise code generation options
- Scripting affine transformations
- [Your crazy idea here]

Scalability: Sub-Polyhedral Approximations



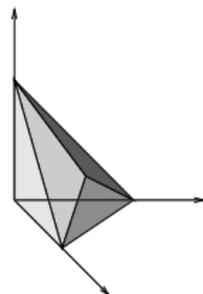
Interval

$$a \leq x_i \leq b$$



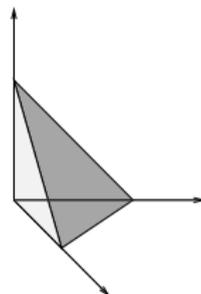
Octagon (UTVPI)

$$\pm x_i \pm x_j \leq c$$



TVPI

$$ax_i + bx_j \leq c$$



Convex Polyhedra

$$\sum a_i x_i \leq c$$

Precision

Intervals \subset Octagons (UTVPI) \subset TVPI \subset Polyhedra

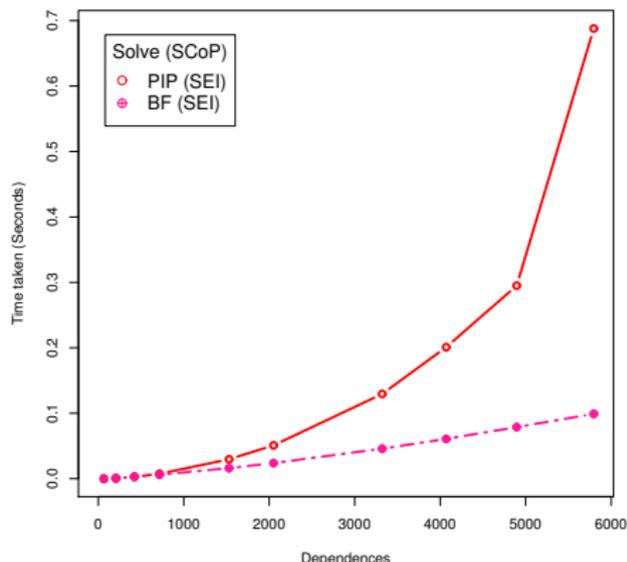
Cost

Scalability: Sub-Polyhedral Approximations

- Replace linear programming (Simplex) with **Bellman Ford**
 $\mathcal{O}(mn^3) \rightsquigarrow \mathcal{O}(mn)$
- Applicable to dependence analysis, code generation:
over-approximation
- Applicable to affine scheduling:
under-approximation
- Preserving feasibility of polyhedra is a tough challenge for some affine scheduling problems

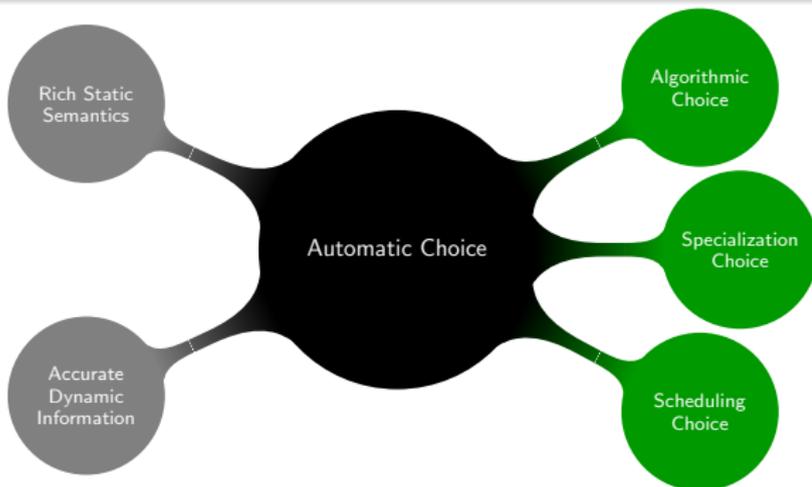
(Unrolled) Gauss-Seidel benchmark
Automatic parallelization with PLuTo

Time taken to Solve System (Seconds) vs. Number of Dependences



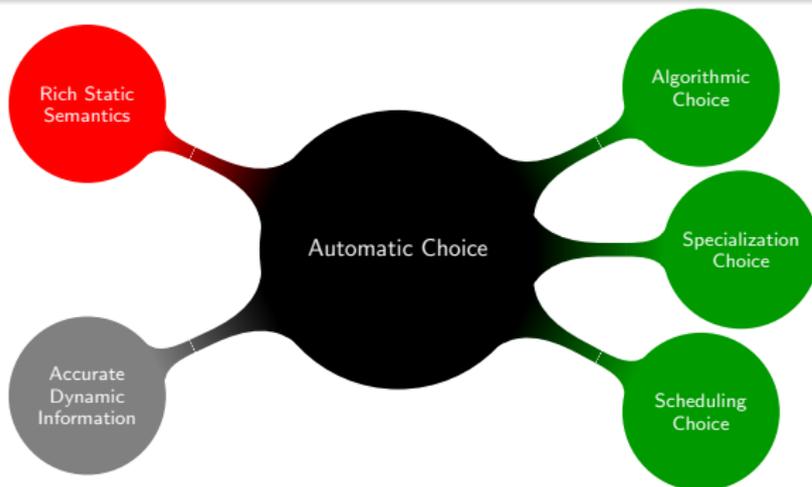
Just-in-Time and Split Compilation

Tools could do a lot better, if provided with enough choice and precise information



Just-in-Time and Split Compilation

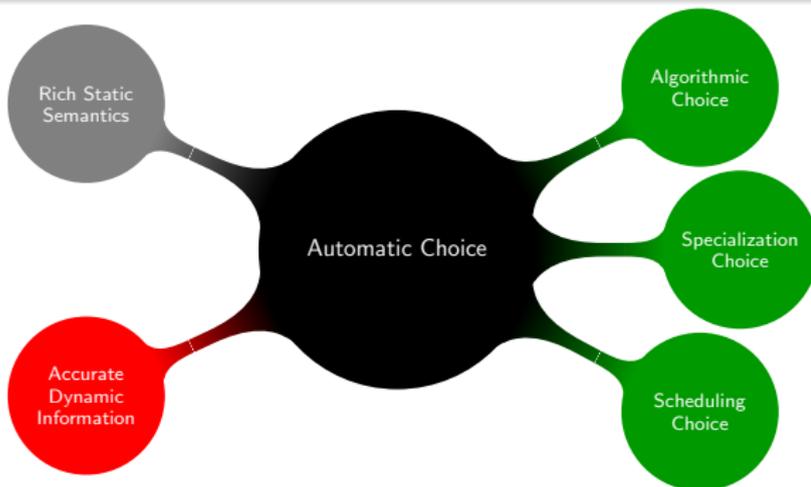
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Importance of **static, non-functional semantics**

Just-in-Time and Split Compilation

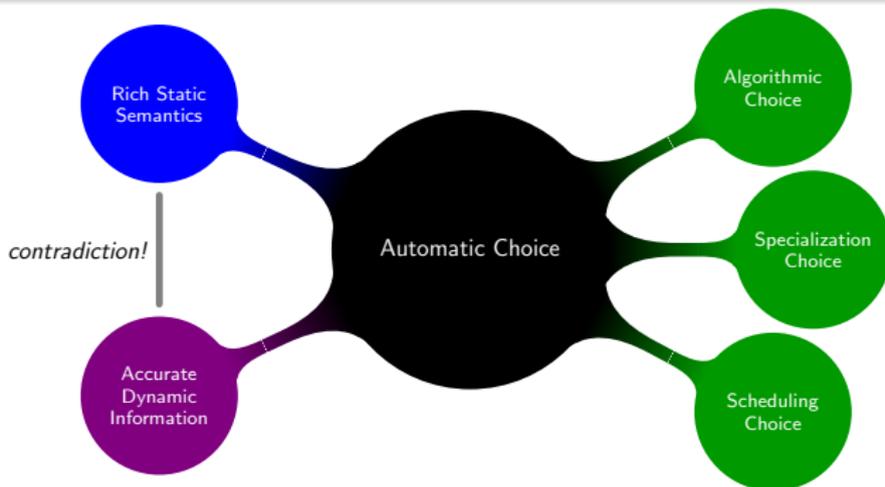
Tools could do a lot better, if provided with enough choice and precise information



Importance of **delaying choice** until information is available

Just-in-Time and Split Compilation

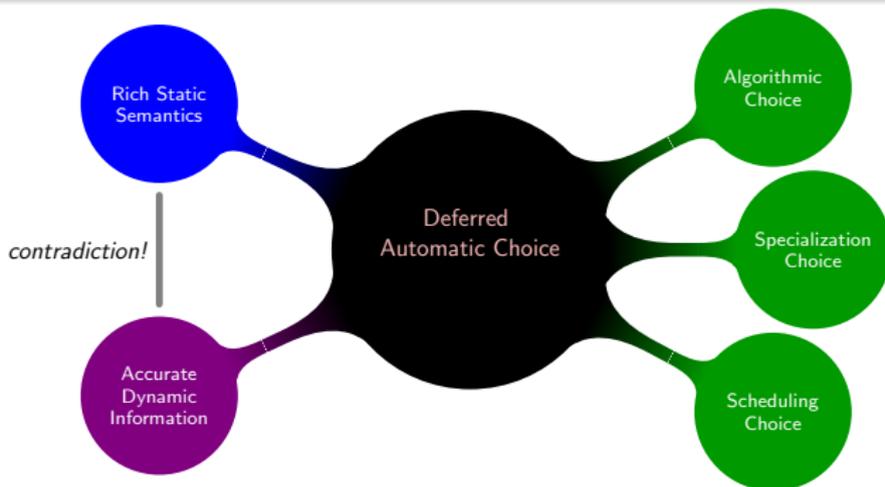
Tools could do a lot better, if provided with enough choice and precise information



Contradiction: accurate information is only available after the most important choices have already been made

Just-in-Time and Split Compilation

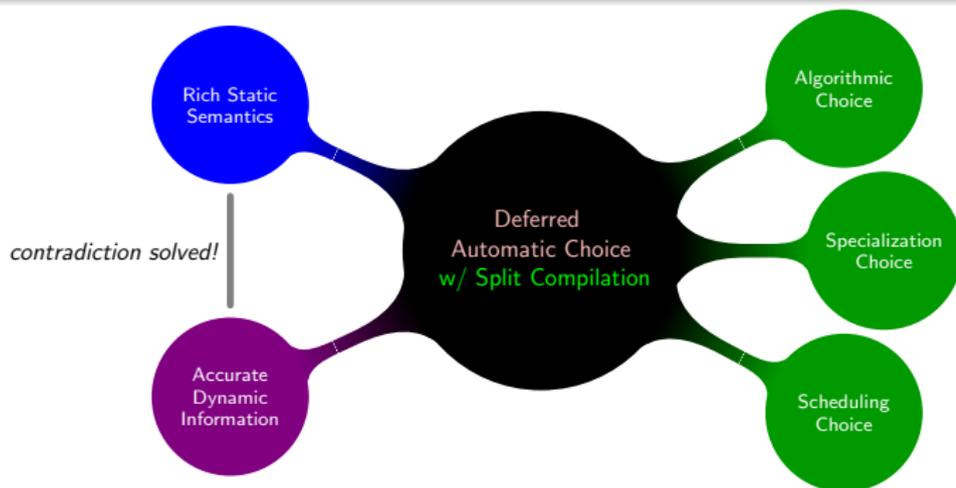
Tools could do a lot better, if provided with enough choice and precise information



Deferred compilation enables Just-in-Time (JIT) optimization when accurate information is available, but loses much of the static semantics carrying choice opportunities

Just-in-Time and Split Compilation

Tools could do a lot better, if provided with enough choice and precise information



Contradiction solved with **split compilation**: *optimizations split over coordinated, offline and online compilation steps, communicating through rich intermediate languages*

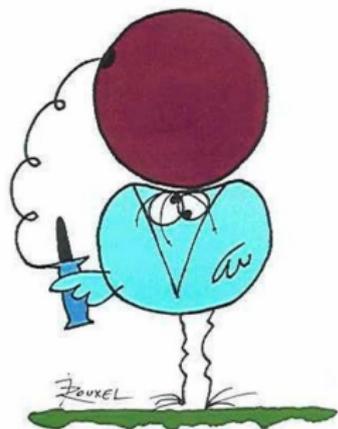
Auto-Tuning, Iterative Optimization, Machine Learning Compilation

Even with rich static semantics and accurate information, **the compiler is left with a huge space of optimization and specialization opportunities**

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Les devises Shadok



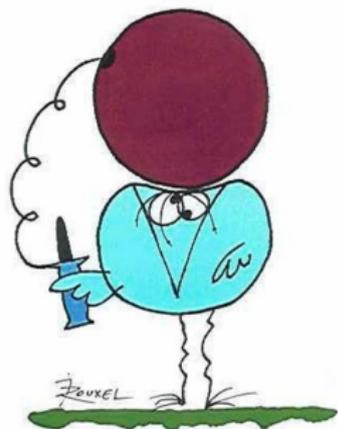
*"By continuously trying, we finally succeed.
Therefore: the more it fails, the more it has chances to work."*

EN ESSAYANT CONTINUELLEMENT
ON FINIT PAR RÉUSSIR. DONC:
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Therefore: the more it fails, the more it has chances to work.”*

Principle of **iterative, feedback-directed optimization**

- Can be embedded transparently in a virtual execution environment

Machine learning techniques for split compilation

- Offline training, feeding online predictive models with target- and application-specific weights
- Leveraging static features in deferred compilation steps



Adopt a Polyhedral Compiler!

It is happening now

- Many blockers have been lifted: better tools, more effective heuristics, better performance, more incentive to reengineer the compilers, more performance to gain, more market impact...
- The expectations are high, much work is awaiting us
- Convince industry to (really) invest into robust platforms, and address open issues, or let's build the software company that will do it

Software

“Production-quality” integer Set Library: <http://freshmeat.net/projects/isl>

→ barvinok, iscc, pet, ppcg, PLuTo, PoCC, Polly (LLVM), Graphite (GCC)